

UNITED STATES DEPARTMENT OF THE INTERIOR BUREAU OF MINES HELIUM ACTIVITY HELIUM RESEARCH CENTER INTERNAL REPORT

MODIFIED REDLICH-KWONG EQU	JATIONS FOR
HYDROGEN AND FOR NE	EON

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HELIUM RESEARCH CENTER INTERNAL REPORT

MODIFIED REDLICH-KWONG EQUATIONS FOR HYDROGEN AND FOR NEON

Ву

Philip C. Tully and Jonnie M Estes

Branch of Fundamental Research
Project 5571
April 1967

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CONTENTS

	Page
Abstract	
Introduction	5
Selection of coefficients	6
Results	8
Hydrogen	11
Neon	12
Other representations of the PVT properties of	
these gases	27
Virials	27
Various other equations	27
Effective critical constants	28
Summary	29
Nomenclature	31
Acknowledgments	32
References	33
ILLUSTRATIONS	
Fig. 1. P vs Z for experimental data and for Z's calculated by the Redlich-Kwong equation	9
2. Percentage absolute difference between experimental Z's for hydrogen and those calculated by the	
modified Redlich-Kwong equation	11

		Page
3.	Percentage absolute difference between experimental Z's for hydrogen and those calculated by the original Redlich-Kwong equation	11
4.	Percentage absolute difference between experimental Z's for neon and those calculated by the modified Redlich-Kwong equation	12
5.	Percentage absolute difference between experimental Z's for neon and those calculated by the original Redlich-Kwong equation	12
	TABLES	
1.	Ranges of experimental conditions over which	
	calculated Z's were compared with	
	experimental Z's	8
2.	Average percentage absolute difference between Z and Z for various forms of the exp calc	
	R-K equation	10
3.	Z-modified Redlich-Kwong vs Z for hydrogen	13
4.	Z-modified Redlich-Kwong vs Z for neon	21
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MODIFIED REDLICH-KWONG EQUATIONS FOR HYDROGEN AND FOR NEON

by

Philip C. Tully $\frac{1}{2}$ and Jonnie M. Estes $\frac{2}{2}$

ABSTRACT

As part of an over-all program to develop a single equation of state for helium and its mixtures to be used in equilibrium thermodynamic consistency calculations, coefficients of the B term of the Redlich-Kwong equation for pure hydrogen and neon are presented. For normal hydrogen, the original Redlich-Kwong (R-K) value of B, which is $\frac{0.0867T_{\rm c}}{P_{\rm c}T}$, is changed to $\frac{0.08063T_{\rm c}}{P_{\rm c}T}$. For temperatures from 98° to 423° K and pressures up to 2,950 atmospheres, this gives an average deviation of 0.63 percent from experimental data. For neon, B is changed to $\frac{0.1025T_{\rm c}}{P_{\rm c}T}$. For temperatures from 120° to 973° K and pressures up to 2,900 atmospheres, this gives an average deviation of 0.48 percent from experimental data. No changes were made in the value of A for either gas.

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INTRODUCTION

The PVT properties of gaseous hydrogen and neon have been represented by various types of equations. It is well known that these two gases do not obey the law of corresponding states and so cannot be well represented by generalized equations of state.

Virial-form equations have been given for hydrogen by Michels, de Graaff, Wassenaar, Levelt, and Louwerse (9). Equations of this

3/ Underlined numbers in parentheses refer to items in the list of references at the end of this report.

type have been used for neon by Michels, Wassenaar, and Louwerse (10); Holborn and Otto (6); Nicholson and Schneider (11); and Sullivan and Sonntag (14). For both of these gases Gunn, Chueh, and Prausnitz (5) have published "effective critical constants" to be used in conjunction with Pitzer's (12) generalized tables.

Goodwin (4) has published a six-constant "approximate widerange equation" for hydrogen. Ziegler, McWilliams, and Keller (16) have redetermined these constants for temperatures to 300° K and pressures to 100 atmospheres.

McCarty and Stewart (8) have developed an 18-constant modified Benedict-Webb-Rubin equation for neon for temperatures from 25° to 300° K and pressures from 0.1 to 200 atmospheres.

This paper presents a modification of the R-K (13) equation of state which is specific for hydrogen. A similar specific modification is made for neon.

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This paper presents a modification of the K-K (12) equation of state which is specific for hydrogen. A similar specific modification is made for neon.

The R-K equation is

$$P = RT/(V-b) - a/T^{1/2}V(V+b)$$
 (1)

or
$$Z = 1/(1-h) - (A^2/B)h/(1+h)$$
, (2)

where
$$Z = PV/RT$$
, (3)

$$A^2 = a/R^2T^{2.5} = 0.4278 T_C^{2.5}/P_CT^{2.5}$$
, (4)

$$B = b/RT = 0.0867 T_{C}/P_{C}T , (5)$$

and
$$h = b/V = BP/Z . (6)$$

Equation 2 can be solved by successive approximations in Z. The work discussed in this paper was done on an IBM 1620 computer. $\frac{4}{}$

4/ Reference to trade names is made for identification only and does not imply endorsement by the Bureau of Mines.

A list of the nomenclature used in this report is appended.

SELECTION OF COEFFICIENTS

Previous papers (2,3) have presented a method for modifying the R-K equation for helium. This modification consists of developing a new coefficient for the B term, and is based on the limiting volume of helium. Similar individualized coefficients are given here for hydrogen and for neon. However, the technique used to determine the new coefficient for helium could not be used for hydrogen and neon because there is no extremely high pressure data for these gases. Although Bridgman's (1) data for hydrogen extend to 13,000 kg/cm²,

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this pressure is not high enough to warrant extrapolation to the limiting volume. We were unable to find any PVT data above 3000 atm for neon.

The selection of the coefficient for hydrogen was based on the data of Michels, de Graaff, Wassenaar, Levelt, and Louwerse (9). The highest (423° K) and lowest (273° K) isotherms at their highest pressure (2,900 atm) were chosen for optimizing the coefficient because we wanted to fit the high pressure data to less than one percent. (The original R-K equation does quite well at low pressures.) Values of Z were calculated at all points along these two isotherms by using numerous B coefficient values near the original (.0867) value. The value of 0.08063 was selected to yield a maximum deviation of < 1 percent at high and low pressures. The optimum value is obviously a function of pressure, but this single value was selected to maintain the simplicity of the equation.

A similar procedure was employed for neon by using the data of Michels, Wassenaar, and Louwerse (10), also at 273° and 423° K. A value of 0.1025 was selected.

The experimental criticals used were $P_{\rm c}$ = 12.80 atm and $T_{\rm c}$ = 33.25° K for hydrogen and $P_{\rm c}$ = 26.86 atm and $T_{\rm c}$ = 44.45° K for neon. This gives

$$B = \frac{.2094}{T}$$
 for hydrogen

$$B = \frac{.1696}{T}$$
 for neon.

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RESULTS

Compressibility factors calculated by using these two coefficients are compared with experimental data over the ranges shown in table 1.

TABLE 1. - Ranges of experimental conditions over which calculated

Z's were compared with experimental Z's

Investigator	Temperature range, °K	Approximate pressure range, atm		
		Min	Max	
	HYDR OGEN			
Michels, de Graaff, Wassenaar, Levelt, and			1/	
Louwerse (9)	273-423	20	$\frac{1}{2425}$ - 2950	
Do	98-248	5	$\frac{1}{2}$ 325-1000	
Johnston and White (7) .	35-300	1	200	
Woolley, Scott and Brickwedde (15)	273-600	20	<u>1</u> / 800-1700	
	NEON			
Michels, Wassenaar, and Louwerse (10)	273-423	25	$\frac{1}{2600}$ -2900	
Holborn and Otto (6)	90-673	1	100	
Nicholson and Schneider (11)	273-973	10	80	
Sullivan and Sonntag (14)	70-120	10	300	

^{1/} Maximum pressure differs with each isotherm.

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Over wide pressure ranges, such as are shown in table 1, plots of P vs Z data for helium, hydrogen, and neon show that dZ/dP goes through a maximum before reaching very high reduced-pressure values (see figure 1). Neither the original R-K equation nor the modifications

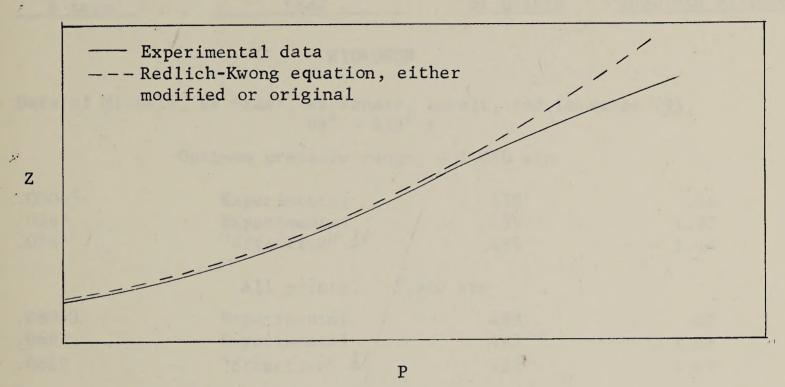


Figure 1. P vs Z for Experimental Data and for Z's Calculated by the Redlich-Kwong Equation

suggested here reproduce this change in slope. Therefore, there is increasing divergence between experimental and calculated values at very high pressures.

The maximum deviation is < 1 percent up to 1,050 atm for hydrogen, (with the exception of a few low temperature points) and up to about 1,500 atm for neon. The average percentage absolute differences over these ranges are given in table 2. For the higher pressure points (up to 2,950 atm), the maximum deviations are considerably greater (< 8.8) than 1 percent. However, the "all-points" averages, also given in table 2, are still < 1 percent. In addition, the table

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TABLE 2. - Average percentage absolute difference between $Z_{\mbox{exp}}$ and $Z_{\mbox{calc}}$ for various forms of the R-K equation

Coefficient, B term	Critical constants used	Number of points	Average percentage absolute difference
	HYDROGEN		
Data of Michels	s, de Graaf, Wassenaar, 1	Corrolt and Laure	(0)
a felocity at	98° - 423° I	K and Louw	erse $(\underline{9})$,
	Optimum pressure range,	< 1.050 atm	
00000		7	
.08063	Experimental	439	.36
.0867	Experimental	439	1.32
.0007	"Effective" 1/	439	1.44
	All points, < 2,95	oo atm	
.08063	Experimental	483	62
.0867	Experimental	483	.63 1.88
.0867	"Effective" 1/	483	1.47
	NEON		
Data of Michels	, Wassenaar, and Louwers	e (10); Nicholso	n and
Schneider (11) ;	and Holborn and Otto (6); 120° - 973°	K
	Optimum pressure range,	< 1.500 atm	
All al - Windows		2,300 acm	
.1025	Experimental	444	.34
.0867	Experimental	444	1.82
.0867	"Effective" 1/	444	1.67
	All points, < 2,90	0 atm.	
1025			
.1025	Experimental	479	.48
	Experimental	479	2.12
.0867	"Effective" 1/	479	1.91

shows the performance of the original R-K equation when two different sets of critical constants are used: (1) the experimental critical constants; and (2) the "effective critical constants" proposed by Gunn, Chueh, and Prausnitz (5), which will be discussed later.

A future paper will discuss the use of these modified equations for mixtures.

Hydrogen

The range of greatest usefulness of the modified equation for hydrogen is shown in figure 2. A similar graph showing how well the

FIGURE 2. - Percentage Absolute Difference Between Experimental Z's for Hydrogen and Those Calculated by the Modified Redlich-Kwong Equation.

unmodified R-K equation fits these same data is shown in figure 3.

FIGURE 3. - Percentage Absolute Difference Between Experimental Z's

for Hydrogen and Those Calculated by the Original Redlich
Kwong Equation.

Down to about 40° K, the low temperature, experimental data of Johnston and White (7) are better represented by the modified equation than by the original. However, since the modified equation gives deviations as large as 2.6 percent at 90°, it is not recommended for use below 98°. Woolley, Scott, and Brickwedde (15) state that the available PVT data

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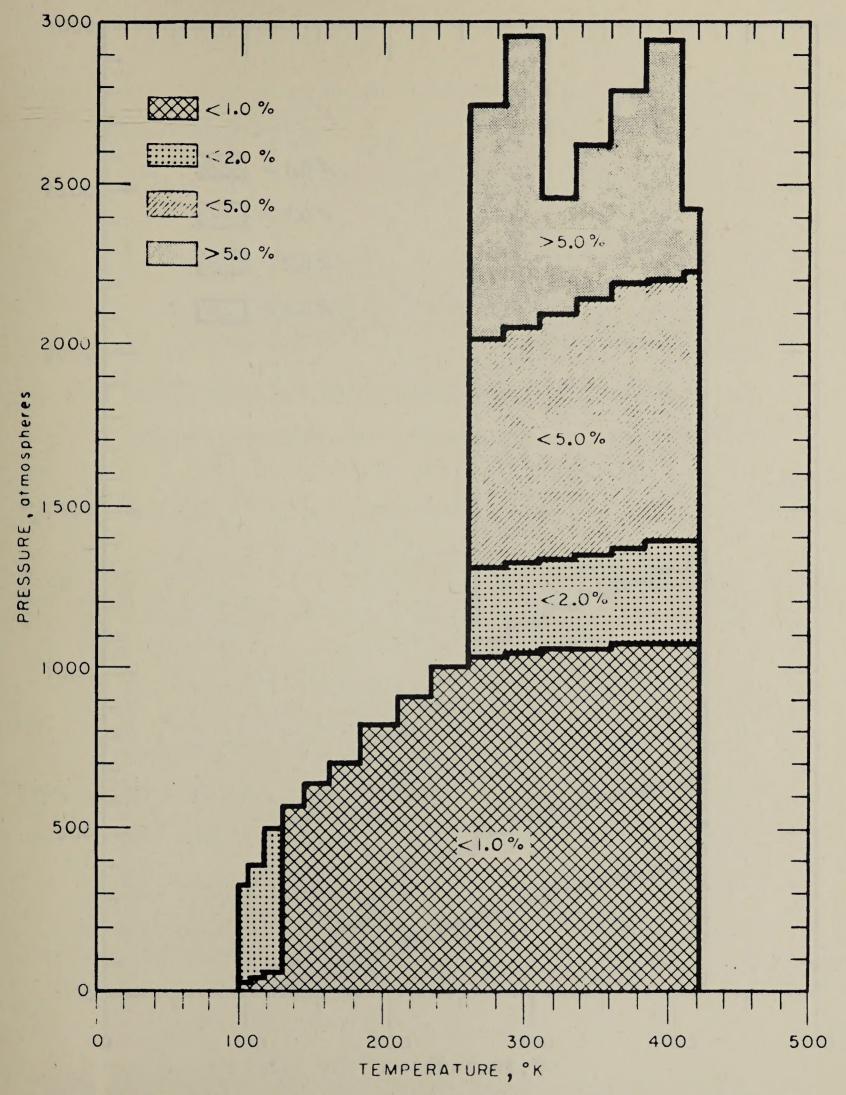
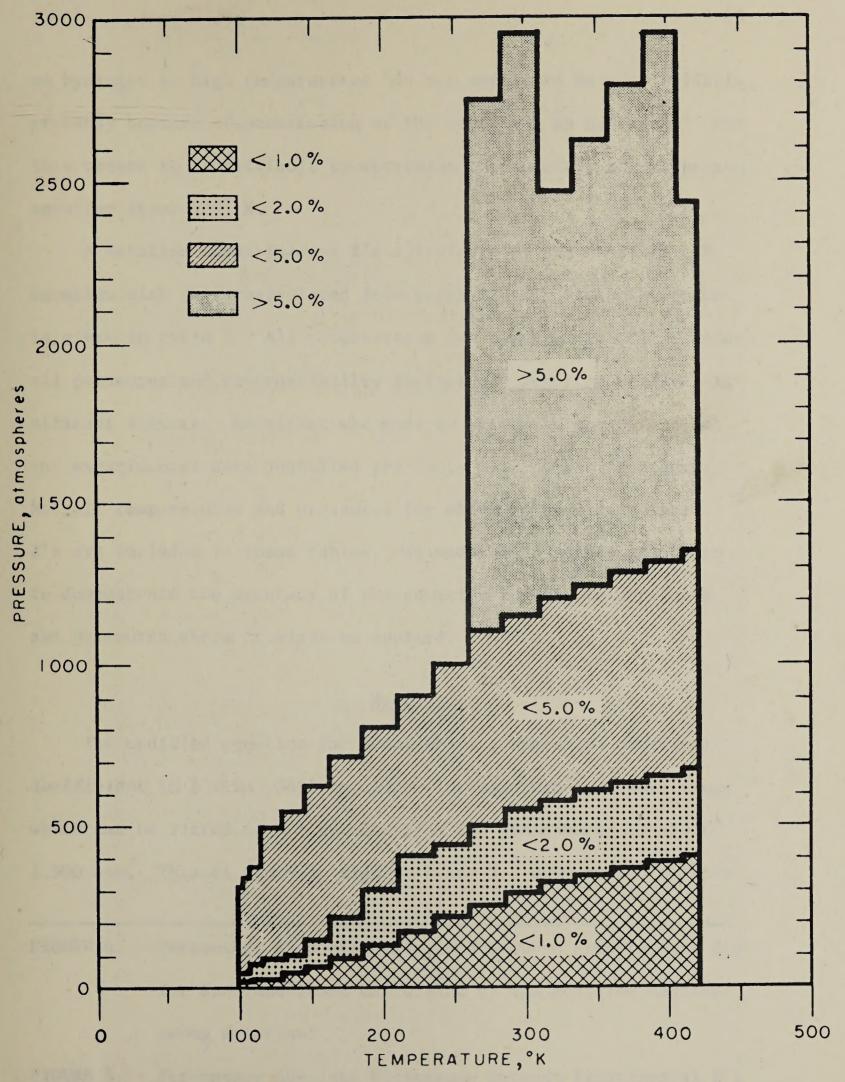
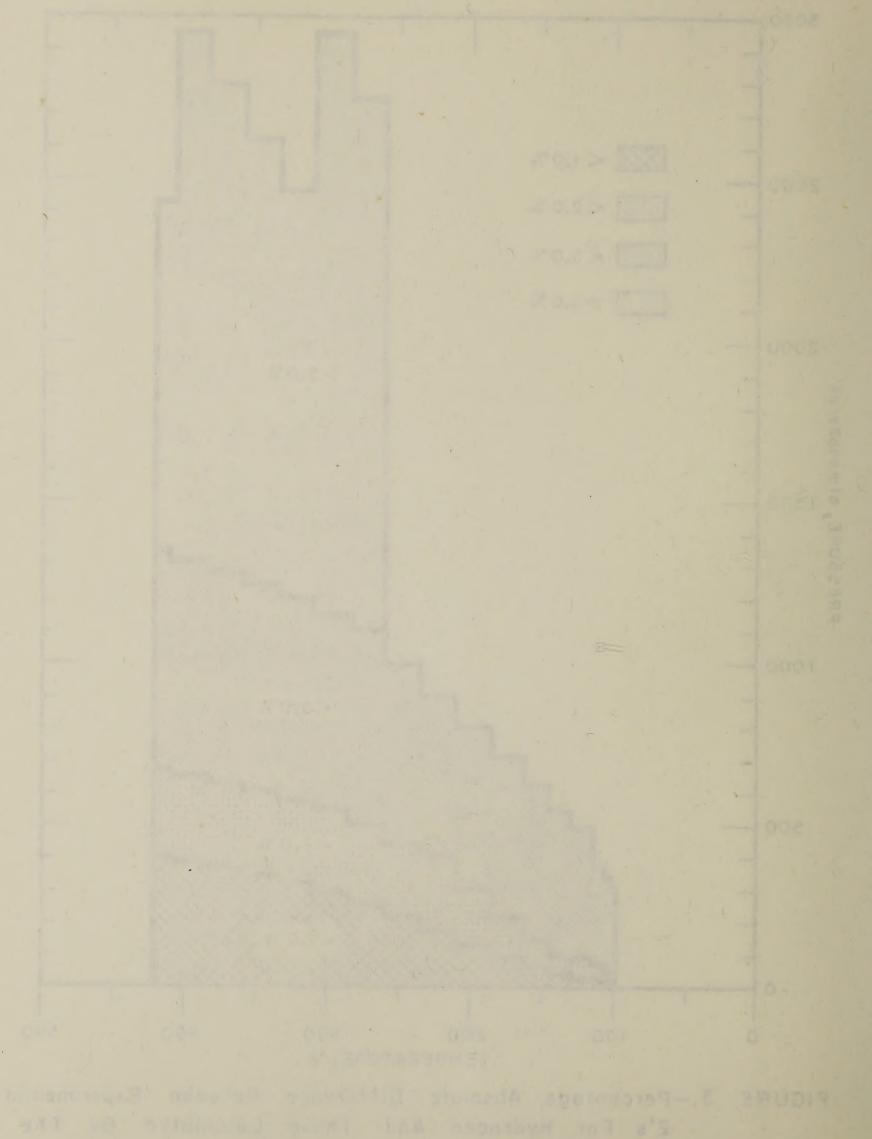


FIGURE 2.— Percentage Absolute Difference Between Experimental Z's For Hydrogen And Those Calculated By The Modified Redlich—Kwong Equation.



Experimental 3.-Percentage Absolute Between FIGURE Difference The Calculated Ву Z's For Hydrogen And Those Original Redlich-Kwong Equation.



on hydrogen at high temperatures "do not appear to be very reliable, probably because of penetration of the container by hydrogen." For this reason it is difficult to determine the accuracy of the present equation above 423° K.

A detailed comparison of Z's calculated by the modified R-K equation with those calculated from experimental data on hydrogen is given in table 3. All temperatures are reported to .01° K, and all pressures and compressibility factors are reported to five significant figures. No effort was made to determine whether or not the experimental data justified precisely this number of figures. Not all temperatures and pressures for which we have calculated Z's are included in these tables. We made an arbitrary selection to demonstrate the accuracy of the equation for the temperatures and pressures where it might be applied.

Neon

The modified equation for neon, which changes the numerical coefficient in B from .0867 to .1025, increases the pressure range which can be fitted to < 1 percent from 100 atmospheres to about 1,500 atm. This is shown in figures 4 and 5. Down to 120° K this

FIGURE 4. - Percentage Absolute Difference Between Experimental Z's for Neon and Those Calculated by the Modified Redlich-Kwong Equation.

FIGURE 5. - Percentage Absolute Difference Between Experimental Z's for Neon and Those Calculated by the Original Redlich-Kwong Equation.

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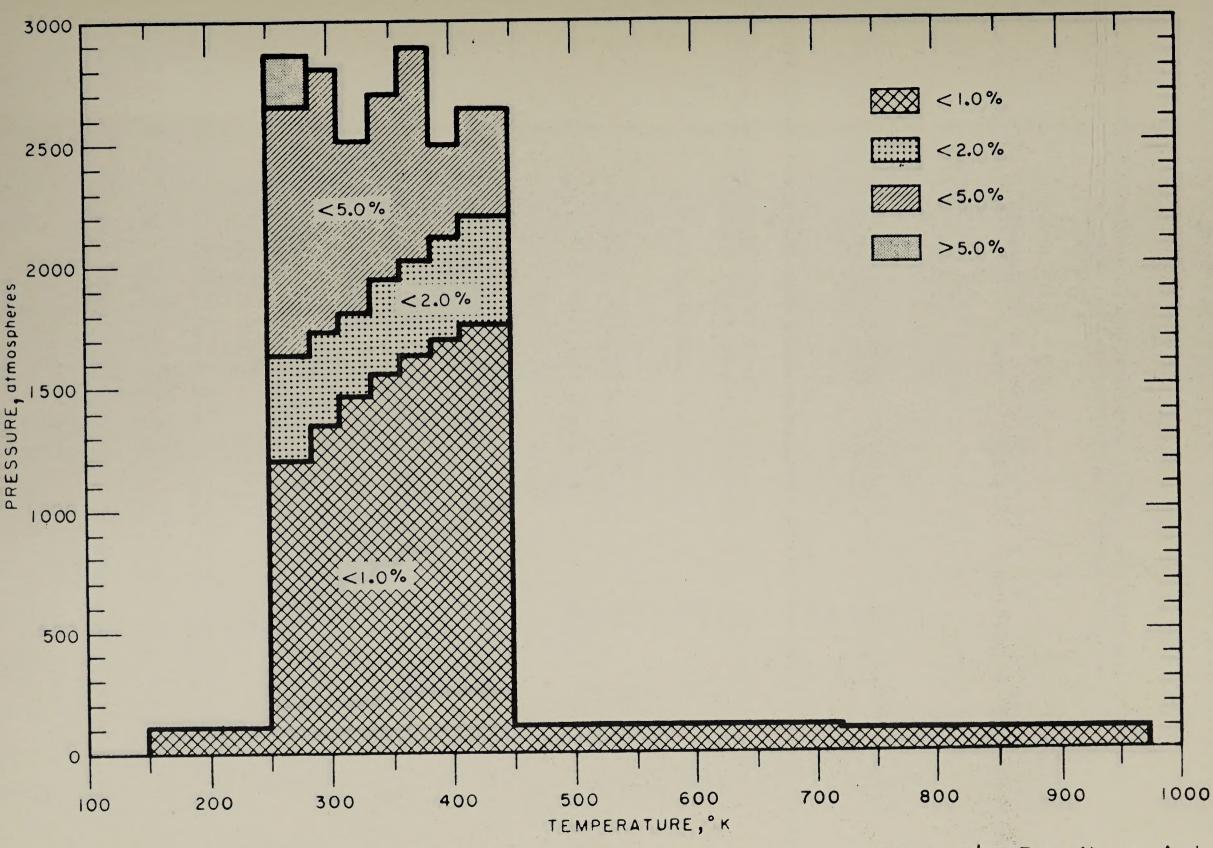
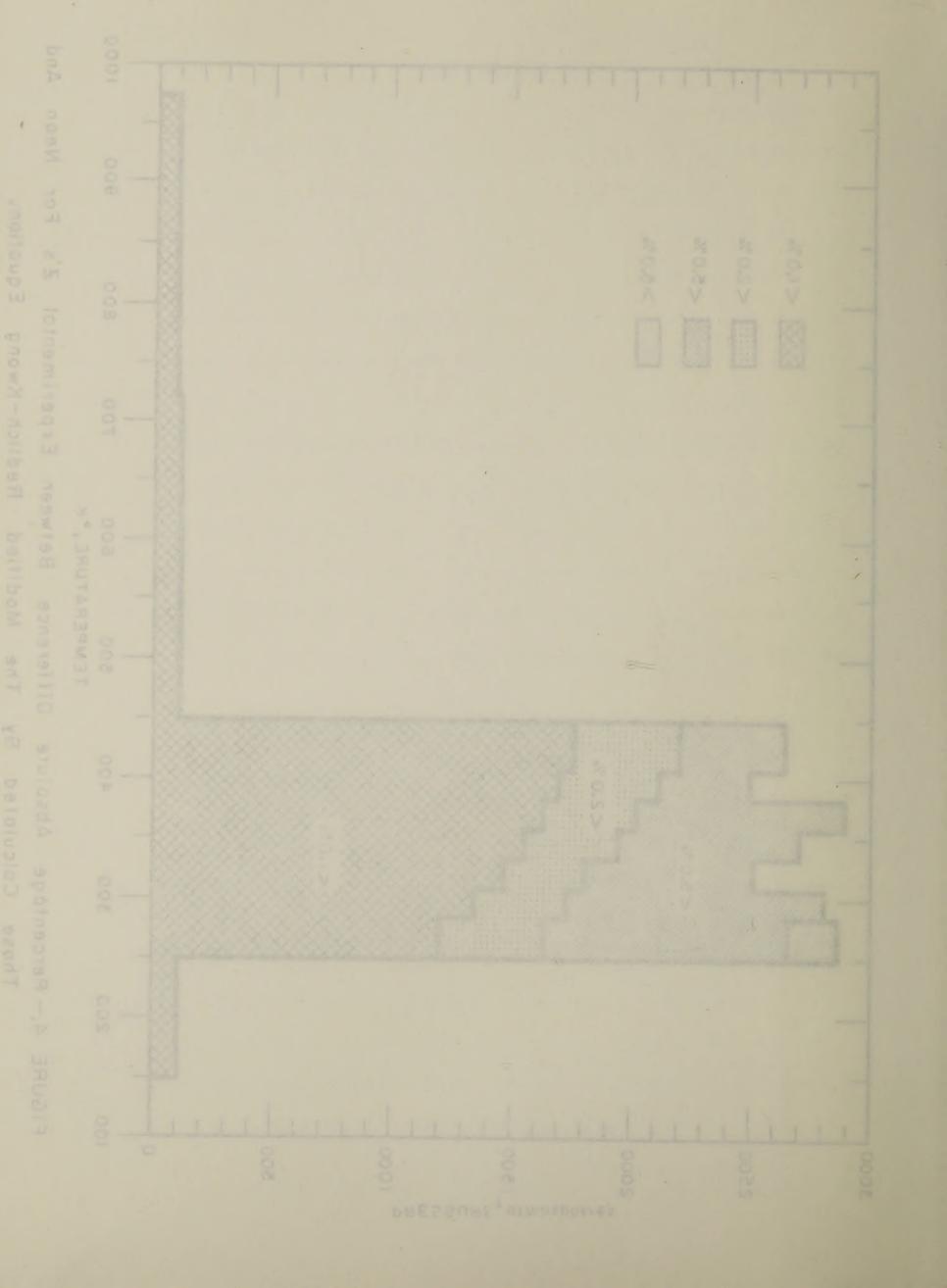


FIGURE 4.— Percentage Absolute Difference Between Experimental Z's For Neon And Those Calculated By The Modified Redlich-Kwong Equation.



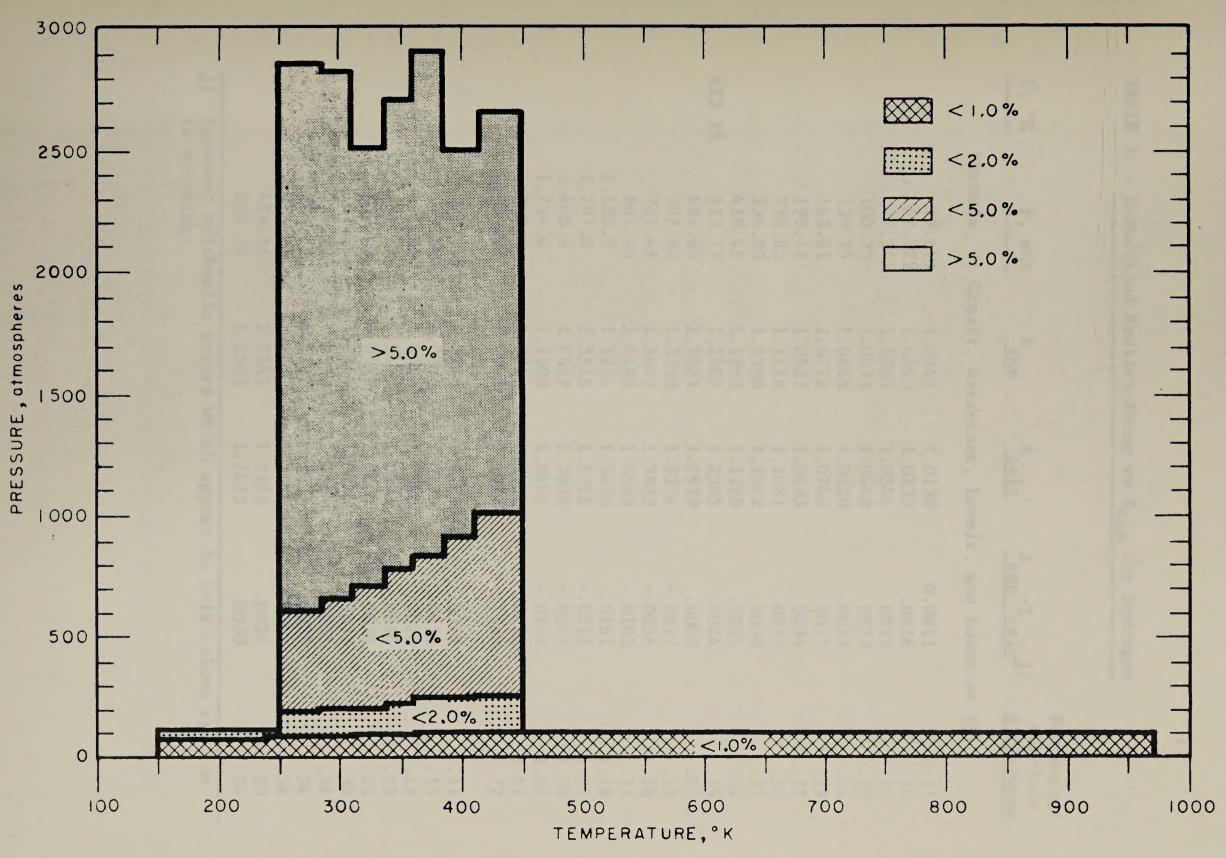


FIGURE 5.—Percentage Absolute Difference Between Experimental Z's For Neon And Those Calculated By The Original Redlich-Kwong Equation.

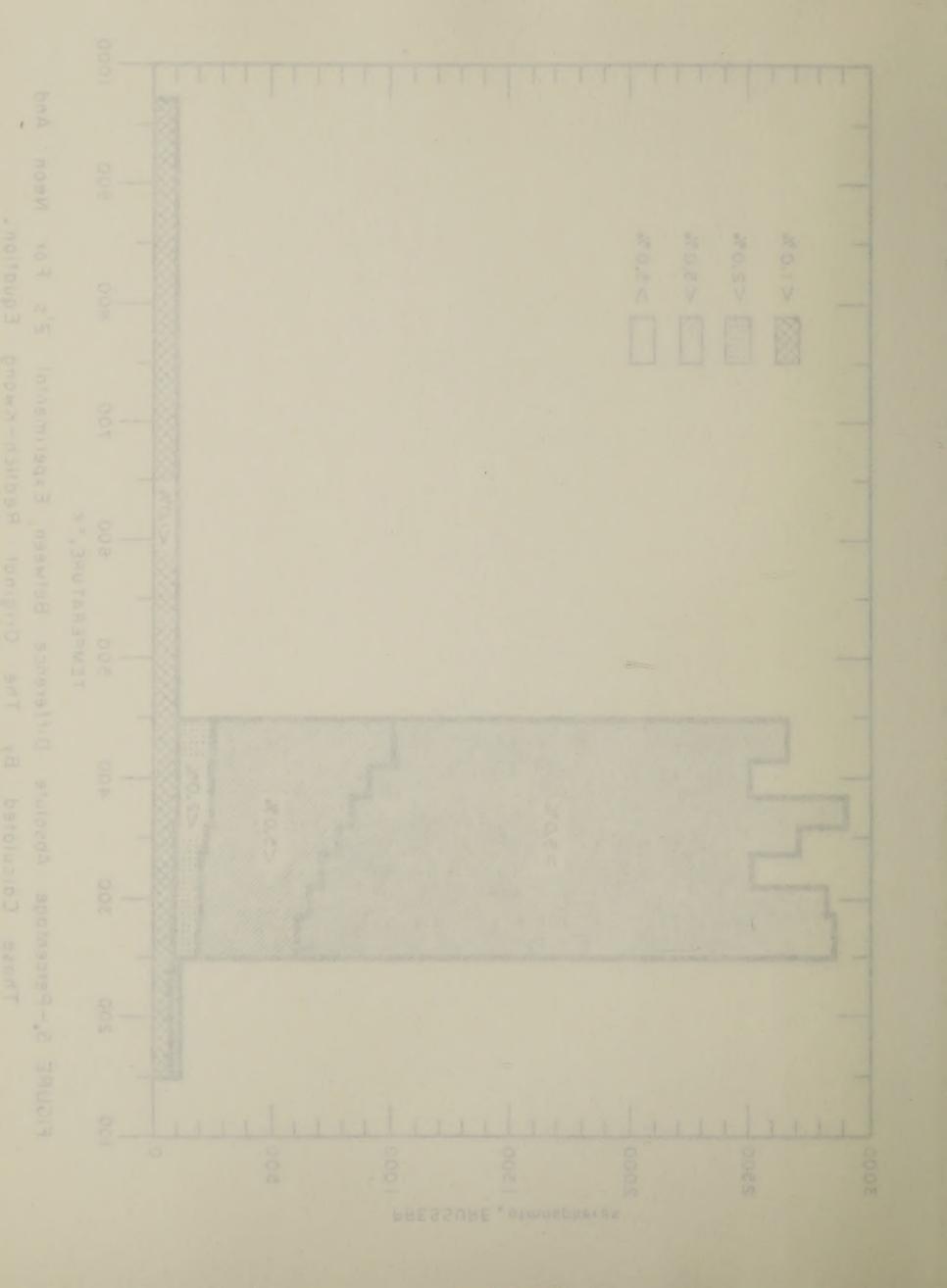


TABLE 3. - Z-Modified Redlich-Kwong vs Zexp for hydrogen

T, °K	P, atm	Zexp	Zcalc	Z _{exp} -Z _{calc} 1/	Percentage absolute difference
	Michels, de Gr	aaff, Wasse	enaar, Leve	elt, and Louwerse	· (<u>9</u>)
	29.671	1.0141	1.0130	0.0011	0.11
	52.722	1.0249	1.0233	.0016	.16
	77.542	1.0363	1.0344	.0019	. 19
	100.73	1.0471	1.0448	.0023	.22
	138.75	1.0648	1.0620	.0027	.26
	165.01	1.0772	1.0740	.0031	.29
	198.12	1.0927	1.0893	.0034	.32
	238.81	1.1118	1.1081	.0037	.33
	336.99	1.1580	1.1542	.0038	. 33
	418.46	1.1963	1.1928	.0035	.29
423.15	513.77	1.2408	1.2385	.0024	. 19
	636.85	1.2981	1.2979	.0002	.01
	707.82	1.3308	1.3324	0017	. 13
	781.48	1.3647	1.3683	0036	.26
	961.96	1.4465	1.4568	0102	.71
	1,138.3	1.5254	1.5436	.0181	1.19
	1,197.0	1.5515	1.5726	0211	1.36
	1,460.6	1.6662	1.7028	0367	2.20
	1,754.6	1.7908	1.8486	0578	3.23
	1,854.4	1.8322	1.8983	0661	3.61
	2,424.1	2.0632	2.1812	1180	5.72
	27.915	1.0140	1.0129	.0011	.11
	49.594	1.0246	1.0230	.0016	. 16
	72.937	1.0360	1.0340	.0020	. 19
	94.739	1.0467	1.0443	.0024	. 23
	130.48	1.0642	1.0614	.0028	.26
398.15	155.16	1.0764	1.0732	.0032	.30
	186.27	1.0919	1.0884	.0035	. 32
	224.51	1.1109	1.1071	.0038	. 34
	316.81	1.1570	1.1528	.0042	.36
	439.36	1.2183	1.2146	.0037	.30
	503.72	1.2503	1.2473	.0030	. 24

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

TABLE 3. - E-Medifited Raditeh-Kwong vs Zava for hydrogen

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TABLE 3. - Z-Modified Redlich-Kwong vs Z_{exp} for hydrogen (Con.)

T, °K	P, atm	Z _{exp}	Zcalc	Z _{exp} -Z _{calc} 1/	Percentage absolute <u>difference</u>
	Michels, de	Graaff, Wass	senaar, Leve	elt, and Louwerse (<u>(9)</u>
	598.95	1.2975	1.2961	0.0014	0.11
	665.82	1.3304	1.3306	0002	.02
	735.25	1.3646	1.3665	0019	. 14
	838.16	1.4147	1.4200	0053	.37
	905.56	1.4472	1.4551	0079	. 54
398.15	1,072.2	1.5271	1.5423	0152	.99
	1,363.7	1.6636	1.6954	0318	1.91
	1,656.8	1.7972	1.8499	0528	2.94
	1,751.6	1.8393	1.8999	0606	3.29
	2,295.0	2.0760	2.1868	1108	5.34
	2,952.5	2.3489	2.5342	1853	7.89
	26.157	1.0138	1.0127	.0011	.11
	46.463	1.0242	1.0226	.0016	.15
	68.324	1.0355	1.0335	.0020	. 19
	88.743	1.0461	1.0437	.0024	.23
	122.21	1.0635	1.0606	.0029	.28
	164.29	1.0856	1.0821	.0036	.33
	210.22	1.1098	1.1058	.0040	.36
	296.57	1.1557	1.1512	.0044	.38
373.15	411.27	1.2168	1.2126	.0042	.34
373.13	560.78	1.2962	1.2939	.0023	. 18
	688.65	1.3638	1.3642	0004	.03
	785.35	1.4144	1.4177	0034	.24
	1,005.6	1.5282	1.5405	0123	.81
	1,280.7	1.6670	1.6946	0276	1.66
	1,647.7	1.8460	1.9012	0551	2.99
	2,163.6	2.0883	2.1920	1037	4.97
	2,791.8	2.3699	2.5464	1765	7.45
			7.7688		
	24.397	1.0135	1.0125	.0010	.10
	43.332	1.0238	1.0223	.0015	.15
348.15	63.713	1.0349	1.0329	.0020	.19
	82.738	1.0454	1.0430	.0024	.23
	and trace to				

 $[\]underline{1}/$ Apparent arithmetic errors which appear in this column are due to rounding.

TABLE 3. - Z-Modified Reditch-Kwong vs Zawn for hydrogen

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TABLE 3. - Z-Modified Redlich-Kwong vs Z for hydrogen (Con.)

T, °K	P, atm	Zexp	Zcalc	Z _{exp} -Z _{calc} 1/	Percentage absolute difference
	Michels, de	Graaff, Wass	senaar, Leve	elt, and Louwerse	<u>(9)</u>
	113.93	1.0626	1.0596	0.0030	0.28
	153.12	1.0844	1.0809	. 0036	. 33
	195.87	1.1084	1.1044	.0040	. 36
	276.25	1.1538	1.1493	. 0045	.39
	383.07	1.2147	1.2102	. 0046	.38
	522.47	1.2944	1.2911	. 0032	. 25
348.15	641.82	1.3623	1.3614	.0009	. 07
	732.21	1.4134	1.4149	0015	.11
	938.46	1.5285	1.5379	0094	. 62
	1,196.8	1.6696	1.6932	0236	1.41
	1,457.7	1.8083	1.8505	0422	2.33
	1,542.7	1.8526	1.9017	0491	2.65
	2,031 1	2.1011	2.1971	0960	4.57
	2,628.7	2.3917	2.5585	1668	6.98
	22 (20	1 0120	1 0100	0010	2.0
	22.638	1.0132	1.0122	.0010	.09
	46.479	1.0268	1.0253	.0015	. 15
	65.669	1.0379	1.0359	.0020	. 19
	90.195	1.0522	1.0497	. 0024	.23
	123.70	1.0719	1.0689	.0030	.28
	160.10	1.0936	1.0900	.0036	.33
	269.41	1.1597	1.1551	.0046	.40
202 15	374.59	1.2242	1.2195	.0047	.39
323.15	520.67	1.3142	1.3108	.0034	.26
	642.27	1.3890	1.3880	.0010	.07
	796.12	1.4827	1.4866	0039	.26
	870.54	1.5276	1.5345	0069	.45
	999.77	1.6049	1.6179	0130	.81
	1,111.8	1.6711	1.6906	0195	1.17
	1,232.2	1.7411	1.7688	0278	1.59
	1,496.4	1.8918	1.9407	0489	2.58
	1,896.6	2.1138	2.2016	0878	4.15
	2,462.7	2.4140	2.5708	1568	6.50

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

TABLE 3. - E-Medified Radiich-Xung ve Zexp for hydrogen

	t in the second		
	1.6906		

Apparent arthmetic errors which appear in this column are due to

TABLE 3. - Z-Modified Redlich-Kwong vs Z_{exp} for hydrogen (Con.)

					Percentage
T, °K	P, atm	7.	7.	z -z 1/	absolute
		Z exp	Zcalc	$\frac{Z_{exp}-Z_{calc}}{1}$	difference
	W4-1-1- 1	C	T	1	
	Michels, de	Graaff, Wass	senaar, Leve	elt, and Louwerse (<u>9)</u>
	20.877	1.0127	1.0119	0.0008	0.08
	42.849	1.0260	1.0246	.0014	. 13
	70.697	1.0431	1.0411	.0020	. 19
	97.295	1.0597	1.0571	.0025	. 24
	121.26	1.0747	1.0718	.0029	.27
	175.51	1.1094	1.1057	.0037	.33
	295.25	1.1878	1.1831	.0047	.39
	395.70	1.2547	1.2500	.0047	.37
298.15	495.16	1.3213	1.3175	.0038	.28
	591.06	1.3855	1.3833	.0022	.16
	733.15	1.4799	1.4818	0020	. 13
	921.87	1.6040	1.6137	0097	.61
	1,138.5	1.7435	1.7661	0226	1.29
	1,385.2	1.8982	1.9402	0421	2.22
	1,760.3	2.1264	2.2054	0790	3.72
	2,294.4	2.4375	2.5833	1 457	5.98
	2,946.3	2.7976	3.0441	2466	8.81
	19.116	1.0122	1.0115	.0007	.07
	39.217	1.0250	1.0238	.0011	. 11
	64.675	1.0415	1.0398	.0017	. 17
	88.967	1.0576	1.0554	.0022	.21
	110.85	1.0724	1.0697	.0026	. 24
	160.34	1.1062	1.1029	.0034	.31
	226.31	1.1525	1.1484	.0041	.35
	314.46	1.2158	1.2112	.0047	.38
273.15	437.10	1.3053	1.3009	.0043	.33
	539.56	1.3805	1.3773	.0032	.23
	669.79	1.4757	1.4756	.0001	.01
	843.30	1.6016	1.6080	0064	.40
	1,043.3	1.7439	1.7615	0176	1.01
	1,272.6	1.9034	1.9384	0350	1.84
	1,622.3	2.1390	2.2085	0695	3.25
	2,123.1	2.4621	2.5956	1335	5.42
	2,736.1	2.8358	3.0690	2332	8.22

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

CABLE 3 - Z-Modified Endilen-Norma wa Zerm for hydrogen (Com.)

Percentage Percentage absolute absolute difference difference difference

Wichels, de Grasif, Wassensst, Levelt, and Louwerse (9)

Apparent orichaetic errors which appear in this column are due to counding.

TABLE 3. - Z-Modified Redlich-Kwong vs Z_{exp} for hydrogen (Con.)

T, °K	P, atm	Zexp	Zcalc	Zexp-Zcalc1/	Percentage absolute difference
	Michels, de	Graaff, Was	senaar, Leve	elt, and Louwerse	(<u>9</u>)
	7.1755	1.0050	1.0045	0.0005	0.05
	28.480	1.0189	1.0182	.0007	.07
	48.181	1.0323	1.0312	.0011	. 11
	88.667	1.0608	1.0589	.0019	. 18
	123.46	1.0859	1.0836	.0023	.21
248.15	186.62	1.1332	1.1301	.0031	.28
240.13	235.16	1.1708	1.1671	.0037	.32
	335.48	1.2503	1.2459	.0044	.35
	425.92	1.3233	1.3190	.0043	.33
	609.50	1.4723	1.4706	.0017	.11
	845.19	1.6619	1.6688	0069	.41
	1,005.6	1.7885	1.8048	0163	. 91
	6.5000	1.0046	1.0043	. 0004	.04
	25.779	1.0177	1.0173	.0004	. 04
	60.785	1.0430	1.0421	.0009	.09
	80.087	1.0574	1.0563	.0011	.10
	111.43	1.0818	1.0803	.0015	. 14
	168.24	1.1277	1.1256	.0021	.18
223.15		1.1645	1.1619	.0026	.23
	302.08	1.2431	1.2397	.0034	.28
	461.19	1.3866	1.3829	.0036	.26
	549.73	1.4672	1.4645	.0027	.18
	642.12	1.5512	1.5505	.0007	. 04
	764.49	1.6616	1.6652	0036	.22
	911.69	1.7928	1.8040	0112	.63
	5.8140	1.0042	1.0039	.0003	.03
	28.994	1.0205	1.0203	.0001	.01
	54.203	1.0394	1.0393	.0001	.01
	99.146	1.0757	1.0756	.0001	.01
198.15		1.1196	1.1192	.0003	.03
270.13	224.48	1.1897	1.1887	.0010	.08
	340.09	1.3047	1.3024	.0023	.18
	488.11	1.4570	1.4543	.0028	. 19
	570.93	1.5429	1.5411	.0018	.12
	370.75	1.5765	T . 7 T T T	.00.20	

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

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TABLE 3. - Z-Modified Redlich-Kwong vs Z exp for hydrogen (Con.)

T, °K	P, atm	Zexp	Zcalc	Zexp-Zcalc 1/	Percentage absolute difference
M:	ichels, de G	raaff, Wass	senaar, Lev	elt, and Louwerse	<u>(9)</u>
198.15	681.22	1.6568	1.6576	-0.0008	0.05
	814.64	1.7931	1.7995	0064	.36
	6.6416	1.0046	1.0045	.0001	.01
	25.460	1.0175	1.0181	0005	. 05
	47.491	1.0342	1.0353	0011	.11
	86.595	1.0668	1.0688	0020	. 18 . 21
173.15	130.20	1.1076	1.1099	0023	.18
	195.12	1.1742	1.1764	0021	. 04
	295.28	1.2865	1.2871	0006 .0015	.10
	424.46	1.4394	1.4379 1.6432	.0013	.07
	594.89	1.6443	1.7885	0021	.12
	713.93	1.7004	1.7003	.0021	. 112
	5.9055	1.0036	1.0038	0002	.02
	30.241	1.0194	1.0213	0019	.18
	55.176	1.0387	1.0418	0031	. 30
	94.388	1.0738	1.0786	0048	.44
153.15	143.55	1.1249	1.1307	0058	.51
	203.71	1.1954	1.2010	0055	.46
	311.07	1.3344	1.3371	0026	.20
	436.39	1.5056	1.5048	.0008	.05
	523.40	1.6258	1.6239	.0019	.12
	630.30	1.7728	1.7718	.0010	.05
	6.3094	1.0034	1.0037	0003	.03
	27.293	1.0151	1.0179	0028	.27
	49.651	1.0312	1.0359	0047	.46
	102.44	1.0799	1.0882	0083	.77
138.15	181.54	1.1750	1.1846	0095	.81
200.25	276.98	1.3106	1.3167	0062	.47
	389.35	1.4818	1.4830	0012	.08
	468.11	1.6042	1.6026	.0016	.10
	565.62	1.7553	1.7524	.0029	.16
123.15	5.6428	.99918	1.0026	0034	. 34

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

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Apparent artichectic errors which appear in this column are due

TABLE 3. - Z-Modified Redlich-Kwong vs Z for hydrogen (Con.)

T, °K	P, atm	Z _{exp}	Zcalc	$\frac{Z_{exp}^{-Z} - Z_{calc}}{2}$	Percentage absolute <u>difference</u>
	Michels, de	Graaff,	Wassenaar,	Levelt, and Louwer	se (9)
	11.257	1.0038	1.0055	-0.0017	0.17
	24.314	1.0068	1.0133	0066	. 65
	44.056	1.0186	1.0280	0094	. 93
	74.689	1.0434	1.0568	0134	1.28
123.15	133.81	1.1104	1.1278	0174	1.57
	201.15	1.2083	1.2250	0167	1.38
	289.84	1.3553	1.3668	0115	.85
	341.05	1.4443	1.4525	0082	.57
	411.23	1.5682	1.5721	0039	.25
	498.98	1.7234	1.7240	0006	.03
	7.9670	1.0013	1.0027	0014	. 14
	22.316	1.0052	1.0094	0043	.43
	55.345	1.0232	1.0338	0106	1.03
	102.33	1.0690	1.0858	0168	1.57
113.15	143.52	1.1249	1.1433	0184	1.64
	216.35	1.2464	1.2615	0151	1.21
	261.76	1.3301	1.3412	0111	. 84
	308.66	1.4199	1.4264	0065	.46
	383.66	1.5663	1.5660	.0003	.02
	7 2712	.99934	1 0009	0015	. 15
	7.2712		1.0008	.0079	. 79
	31.162 61.248	1.0016	1.0326	0154	1.51
	91.635	1.0464	1.0670	0206	1.97
103.15	127.96	1.0962	1.1194	0232	2.12
103.13	192.36	1.2110	1.2309	0199	1.64
	232.84	1.2929	1.3082	0153	1.18
	274.92	1.3819	1.3918	0098	.71
	342.84	1.5294	1.5306	0012	.08
	6.9217	.99821			. 16
	11.566	.99715		0030	.30
4000	29.547	. 99649		0087	.87
98.15	47.235	1.0017	1.0157	0140	1.40
	69.428	1.0162	1.0360	0197	1.94
	101.60	1.0521	1.0768	0247	2.35
	120.09	1.0791	1.1050	0259	2.40

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

TARLE 3. - E-Modified Redlich-Ewong vs Z exp for hydrogen

Apparent erithmetic errors which appear in this column are due to rounding.

TABLE 3. - Z-Modified Redlich-Kwong vs Z for hydrogen (Con.)

T, °K	P, atm	z _{exp}	z _{calc}	Z _{exp} -Z _{calc} 1/	Percentage absolute difference
	Michels, de	Graaff, Was	ssenaar, Le	velt, and Louwers	e (<u>9</u>)
98.15	151.31 218.10 257.73 322.04	1.1332 1.2702 1.3588 1.5068	1.1584 1.2881 1.3706 1.5089	-0.0252 0179 0118 0022	2.22 1.41 .87 .14
	20.000	Johnston	and White	(7)	
	1.0000 10.000 20.000 30.000	1.0001 .99416 .98942 .98726	.99956 .99672 .99583 .99732	.0006 0026 0064 0101	.06 .26 .65
90.00	40.000 60.000 80.000 100.00 150.00 200.00	.98793 .99673 1.0142 1.0388 1.1315 1.2430	1.0012 1.0154 1.0374 1.0658 1.1562 1.2629	0132 0187 0232 0270 0247 0198	1.34 1.87 2.29 2.60 2.19 1.60

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

equation. Below this temperature, however, the original equation should be used. All indications are that this modified equation can be used at temperatures much higher than 423° K and pressures higher than the 100 atm shown in figure 4.

A detailed comparison of experimental Z's with those calculated by this modification is shown in table 4, which was compiled on the same basis as table 3.

TARLE 3. - 2-Modiline Sedilen-Swang vs Z .. 5 Steam

		151.31 218.10 237.73 222.04	
.05 .26 .65			
		80,000 80,000 100,00 200,00	

Ly Apparent artifactic errors which appear in this colony are due to te roundings

and illestion gives a bester fit to experiment data than the original aquation of the united by used. All indications are that this modified equation out to used at temperatures can't then \$12." I and pressures higher than \$2.2." I and pressures higher than \$2.0. I am shown in figure.

A described comparts on of experimental 2 a with those coloulated by this modification is shown in each to which was compiled on the same basis or tools 3.

TABLE 4. - Z-Modified Redlich-Kwong vs Z for neon

т, °к	P, atm	Zexp	Zcalc	Zexp-Zcalc1/	Percentage absolute difference
	. Milima	Nicholson a	and Schneide	er (<u>11</u>)	
973.15	20.000 40.000 60.000 80.000	1.0030 1.0065 1.0100 1.0135	1.0033 1.0067 1.0100 1.0134	-0.0004 0002 0001 .0001	0.04 .02 .01 .01
873.15	20.000 40.000 60.000 80.000	1.0034 1.0072 1.0111 1.0150	1.0037 1.0074 1.0111 1.0148	0004 0002 0000 .0001	.03 .02 .00 .01
773.15	20.000 40.000 60.000 80.000	1.0038 1.0081 1.0125 1.0168	1.0041 1.0083 1.0124 1.0166	0003 0001 .0000 .0002	.03 .01 .00 .02
		Holborn	and Otto (6	<u>(</u>)	
673.09	1.3157 26.316 52.632 78.947 105.26	1.0001 1.0063 1.0128 1.0194 1.0259	1.0003 1.0062 1.0124 1.0186 1.0248	0002 .0001 .0004 .0008 .0011	.02 .01 .05 .08
573.10	1.3157 26.316 52.632 78.947 105.26	1.0001 1.0075 1.0152 1.0229 1.0306	1.0004 1.0071 1.0142 1.0214 1.0286	0002 .0004 .0009 .0015 .0020	.02 .04 .09 .14
473.12	1.3157 26.316 52.632 78.947 105.26	1.0002 1.0086 1.0178 1.0270 1.0364	1.0004 1.0083 1.0167 1.0252 1.0337	0002 .0003 .0011 .0018 .0027	.02 .03 .10 .17 .26

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

TABLE 4. - Z-Modified Sadilah-Kwong vs Z .. for near

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^{1/} Appacent srithmetic errors which appear in this column are due co rounding.

TABLE 4. - Z-Modified Redlich-Kwong vs Z for neon (Con.)

T, °K	P, atm	Zexp	Zcalc	Z _{exp} -Z _{calc} 1/	Percentage absolute difference
	Miche	els, Wassena	aar, and Lo	uwerse (<u>10</u>)	
	37.568	1.0146	1.0130	0.0016	0.16
	61.434	1.0236	1.0214	.0022	.22
	86.687	1.0332	1.0303	.0030	.29
	114.21	1.0436	1.0400	.0036	.34
	132.69	1.0508	1.0467	.0041	.39
	155.22	1.0594	1.0548	.0046	.44
	192.63	1.0738	1.0683	.0054	.50
	229.82	1.0880	1.0819	.0060	.56
	268.87	1.1030	1.0963	.0067	.61
	304.07	1.1167	1.1094	.0074	.66
	353.51	1.1356	1.1278	.0078	.68
423.15	415.64	1.1597	1.1513	.0084	.72
423.13	503.86	1.1938	1.1848	.0090	.75
	599.41	1.2306	1.2215	.0090	. 74
	688.32	1.2648	1.2560	.0088	.70
	772.51	1.2971	1.2887	.0083	. 64
	825.92	1.3172	1.3097	.0075	.57
	950.25	1.3643	1.3585	.0057	.42
	1,154.0	1.4412	1.4391	.0020	. 14
	1,479.7	1.5620	1.5689	0068	.44
	1,762.9	1.6651	1.6824	0172	1.04
	2,039.7	1.7642	1.7934	0291	1.65
	2,210.0	1.8245	1.8619	0374	2.05
	2,635.5	1.9733	2.0332	0598	3.03
	35.339	1.0144	1.0128	.0016	. 15
	57.781	1.0232	1.0210	.0021	.21
	81.523	1.0327	1.0298	.0029	.28
	112.90	1.0452	1.0415	.0037	.35
	140.17	1.0561	1.0518	.0043	.40
398.15	161.54	1.0647	1.0599	.0047	.44
	181.06	1.0726	1.0674	.0052	.49
	215.99	1.0867	1.0808	.0059	. 54
	252.67	1.1017	1.0951	.0066	.60
	309.79	1.1249	1.1175	.0074	.66
	390.46	1.1578	1.1495	.0083	.72

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

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Apparent arithmetic errors which appear in this column ere due to rounding.

TABLE 4. - Z-Modified Redlich-Kwong vs Z exp for neon (Con.)

T, °K	P, atm	Zexp	Zcalc	Zexp-Zcalc 1/	Percentage absolute difference
	Michels, Was		Louwerse (
	473.26	1.1917	1.1828	0.0089	0.75
	562.97	1.2283	1.2193	.0090	.74
	683.43	1.2773	1.2688	.0086	.67
	775.69	1.3147	1.3070	.0077	.59
	892.58	1.3620	1.3558	.0062	.46
398.15	1,122.6	1.4542	1.4524	.0017	.12
	1,468.2	1.5905	1.5988	0084	.53
	1,657.6	1.6640	1.6795	0155	.93
	1,927.4	1.7672	1.7947	0275	1.56
	2,079.9	1.8249	1.8598	0349	1.91
	2,482.4	1.9754	2.0320	0 566	2.87
	33.109	1.0140	1.0126	.0014	. 14
	54.126	1.0227	1.0207	.0020	.20
	76.345	1.0319	1.0293	.0026	.25
	100.57	1.0422	1.0388	.0034	.32
	131.23	1.0550	1.0510	.0040	.38
	151.23	1.0635	1.0590	. 0046	.43
	202.15	1.0852	1.0796	.0056	.52
	267.31	1.1132	1.1064	.0068	.62
	310.72	1.1319	1.1245	.0074	.65
	442.56	1.1891	1.1804	.0086	.72
373.15	526.34	1.2253	1.2166	.0087	.71
	639.01	1.2743	1.2658	.0085	.67
	725.20	1.3115	1.3038	.0077	.59
	834.58	1.3588	1.3523	.0064	.47
	1,049.8	1.4510	1.4487	.0023	.16
	1,300.9	1.5574	1.5621	0047	.30
The state of the	1,551.5	1.6618	1.6758	0140	. 84
	1,805.1	1.7660	1.7913	0253	1.44
	1,948.7	1.8243	1.8569	0325	1.78
	2,327.5	1.9762	2.0298	0536	2.71
	2,894.5	2.1976	2.2891	0916	4.17
348.15	30.881	1.0137	1.0123	.0014	. 14

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

TABLE 4. - 2-Modified Medilion-Name vs 2 and for neon

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i/ Apparent arithmetic errors which appear in this column are due to rounding.

TABLE 4. - Z-Modified Redlich-Kwong vs Z exp for neon (Con.)

T, °K	P, atm	Zexp	Zcalc	$\frac{Z_{exp}-Z_{calc}}{2}$	Percentage absolute <u>difference</u>
	Miche	ls, Wassena	ar, and Lou	werse (<u>10</u>)	
	50.475 71.182 98.538	1.0222 1.0312 1.0432	1.0202 1.0287 1.0400	0.0019 .0025 .0032	0.19 .25 .31
	122.30 157.90 188.30	1.0538 1.0698 1.0835	1.0499 1.0650 1.0781	.0039 .0047 .0054	.37 .44 .50
	220.20 269.85 339.93	1.0980 1.1206 1.1527	1.0919 1.1137 1.1450	.0061 .0068 .0077	.55 .61 .67
348.15	439.26 562.26 667.82	1.1986 1.2558 1.3044	1.1902 1.2472 1.2968	.0084 .0086 .0077	.70 .68
	776.24 943.06 1,210.8	1.3546 1.4315 1.5536	1.3482 1.4280 1.5575	.0064 .0035 0038	.59 .47 .24
	1,444.8 1,682.0 1,816.4	1.6586 1.7637 1.8226	1.6713 1.7871 1.8528	0127 0234 0303	.25 .76 1.32
	2,171.5 2,704.8	1.9762 2.2010	2.0267 2.2883	0505 0873	1.66 2.56 3.97
	28.652 53.146 73.369	1.0133 1.0244 1.0337	1.0120 1.0224 1.0311	.0013 .0020 .0026	.13
	91.354 118.00 146.30	1.0420 1.0546 1.0679	1.0390 1.0508 1.0635	.0030	.25 .29 .36
323.15	174.43 203.93 254.90	1.0813 1.0955 1.1202	1.0763 1.0899	.0044 .0050 .0056	.41 .46 .52
	314.61 452.95 583.32	1.1494	1.1137 1.1421 1.2097	.0065 .0073 .0080	.58 .63 .65
	717.71 903.14	1.2825 1.3493 1.4414	1.2749 1.3432 1.4386	.0076 .0061 .0027	.59 .46 .19

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

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Apparent arithmetic errors which appear in this column are due to rounding.

TABLE 4. - Z-Modified Redlich-Kwong vs Z exp for neon (Con.)

T, °K	P, atm	Zexp	Zcalc	Z _{exp} -Z _{calc} 1/	Percentage absolute difference
	Miche	ls, Wassena	ar, and Lou	werse (<u>10</u>)	
	1,120.0	1.5483	1.5515	-0.0032	0.21
	1,337.2	1.6538	1.6654	0115	.70
323.15	1,557.7	1.7597	1.7814	0217	1.24
	1,682.7	1.8191	1.8474	0283	1.56
	2,013.2	1.9739	2.0219	0480	2.43
	2,512.7	2.2028	2.2861	0833	3.78
	26.424	1.0129	1.0116	.0013	.13
	48.997	1.0237	1.0217	.0020	.19
	67.617	1.0325	1.0301	.0024	.23
	92.974	1.0450	1.0419	.0031	.30
	114.82	1.0557	1.0522	.0036	.34
	134.68	1.0655	1.0616	.0039	.37
	160.52	1.0785	1.0741	.0044	.41
	187.61	1.0923	1.0874	.0050	.45
	211.96	1.1048	1.0994	.0053	.48
	289.18	1.1451	1.1386	.0065	.57
298.15	373.29	1.1894	1.1824	.0071	.59
	477.39	1.2450	1.2378	.0071	.57
	572.54	1.2959	1.2895	.0064	.49
	828.89	1.4338	1.4316	.0022	. 15
	1,028.4	1.5408	1.5441	0033	.22
	1,228.4	1.6467	1.6576	0109	. 66
	1,425.7	1.7501	1.7702	0201	1.15
	1,547.6	1.8132	1.8400	0267	1.47
	1,853.9	1.9701	2.0155	0454	2.30
	2,317.4	2.2020	2.2813	0793	3.60
	2,824.1	2.4487	2.5721	1234	5.04
	24.194	1 0122	1 0111	0010	
	50.228	1.0123 1.0250	1.0111	.0012	.12
	76.959	1.0385	1.0233	.0017	. 17
273.15	99.321	1.0502	1.0363	.0022	.21
	123.06		1.0473	.0028	. 27
	146.61	1.0626	1.0593	.0033	.31
	140.01	1.0752	1.0714	.0038	.36

^{1/} Apparent arithmetic errors which appear in this column are due to rounding

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		118.778	
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TABLE 4. - Z-Modified Redlich-Kwong vs Z_{exp} for neon (Con.)

T, °K	P, atm	Zexp	Zcalc	$\frac{Z_{exp}-Z_{calc}}{2}$	Percentage absolute difference
	Miche	ls, Wassena	ar, and Louw	verse (<u>10</u>)	
	171.27	1.0885	1.0843	0.0042	0.20
	209.65	1.1096	1.1047	.0042	0.39
	263.68	1.1397	1.1342	.0055	.44 .48
	318.99	1.1708	1.1650	.0058	.49
	434.66	1.2373	1.2315	.0059	.47
	599.38	1.3331	1.3291	.0040	.30
	728.12	1.4087	1.4069	.0018	.13
273.15	935.85	1.5305	1.5344	0039	.26
	1,118.5	1.6366	1.6476	0109	.67
	1,299.1	1.7407	1.7601	0195	1.12
	1,410.9	1.8044	1.8299	0255	1.41
	1,691.7	1.9623	2.0058	0435	2.22
	2,118.2	2.1970	2.2731	0761	3.46
	2,586.7	2.4482	2.5670	1189	4.86
	2,865.7	2.5945	2.7416	1471	5.67
		Ho1borr	and Otto (<u>6</u>)	
	1.3157	1.0004	1.0006	0002	0.2
	26.316	1.0131	1.0130	.0002	.02
223.16	52.632	1.0272	1.0266	.0002	.06
	78.947	1.0418	1.0409	.0008	.08
	105.26	1.0570	1.0558	.0011	.11
	1.3157	1 0000	1 0006	ns they builded	
	26.316	1.0003	1.0006	0003	.03
173.17	52.632	1.0123 1.0258	1.0126	0004	.04
	78.947	1.0238	1.0269	0011	.10
	105.26	1.0562	1.0426	0021	. 20
	103.20	1.0302	1.0596	0035	.33
		Sullivan	and Sonntag	<u>(14</u>)	*
	10.114	1.0014	1.0012	.0001	.01
120.0	29.444	1.0054	1.0058	0004	.04
	50.451	1.0117	1.0138	0021	.21

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

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TABLE 4. - Z-Modified Redlich-Kwong vs Z for neon (Con.)

T, °K	P, atm	Zexp	Z	Z _{exp} -Z _{calc} 1/	Percentage absolute difference
		Sullivan a	and Sonntag	(<u>14</u>)	
120.0	72.576 105.30 155.56 239.07 304.79	1.0206 1.0385 1.0760 1.1599 1.2386	1.0256 1.0485 1.0941 1.1889 1.2735	-0.0049 0100 0181 0290 0349	0.48 .96 1.68 2.50 2.82

^{1/} Apparent arithmetic errors which appear in this column are due to rounding.

OTHER REPRESENTATIONS OF THE PVT PROPERTIES OF THESE GASES

Virials

The virial-form equations mentioned in the Introduction naturally give a far better fit to the discrete isotherms they represent than do the two modified equations. No two-constant equation developed for a wide temperature range can be expected to achieve the same degree of accuracy as a six-constant equation designed to fit a single isotherm. The usefulness of these modified R-K equations lies in their ability to predict data over large ranges of pressure and temperature. Within certain limitations, they are also useful for mixtures.

Various Other Equations

The six-constant equations of Goodwin (4) and of Ziegler, McWilliams, and Keller (16) for hydrogen have been used to calculate volumes which were compared with experimental volumes taken from Michels, de Graaff,

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OTHER ANTERSENTATIONS OF THE PAT ENGLISHING

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Various Other Squartery

The six-constant equations of Goodwin (4) and of Riegier, McWilliams, and Keller (16) for hydrogen have been unid to calculate volumes which the compared with experimental volumes taken from Michels, de Graeff,

Wassenaar, Levelt, and Louwerse (9) and from Johnston and White (7). Because the work of Ziegler, McWilliams, and Keller consisted of a redetermination of Goodwin's constants, their equation gave a lower average percentage absolute deviation, as might have been expected. For temperatures of 100° K and below, their equation fits experimental data better than our modified R-K; above 100° the modified R-K fits better.

McCarty and Stewart's (8) equation for neon gives a better fit to experimental data than the modified R-K does in the temperature and pressure ranges for which their 18-constant equation was developed. At pressures and/or temperatures above this range the modified R-K fits experimental data better.

Effective Critical Constants

Gunn, Chueh, and Prausnitz (5) say "...Effective critical constants for helium and normal hydrogen have been determined by fitting experimental volumetric data for these gases to the generalized tables of Pitzer (12). The effective critical temperature and pressure are found to depend on the temperature and on the molecular mass in a simple manner ...".

For hydrogen they give

$$T_c = \frac{43.6}{1 + \frac{21.8}{(1.008)(T)}}$$
 and $P_c = \frac{20.2}{1 + \frac{44.2}{(1.008)(T)}}$.

Similar equations are indicated for neon.

Of the various methods (other than virials) for representing

Messenser, Levelt, and Louverse (2) and from Johnston and White (1).

Because the work of Sieglar, McMilliams, and Kallar consisted of a

redatermination of Goodwin's constants, their equation gave a lover

average percentage absolute deviation, as might have buen expected.

For comporatures of 100' K and below, their equation fits expect
mental data better than our modified N-K; above 100' the modified

R-K firs better.

Haddery and Simmer's (3) equalities for name a better

fit to experimental data then the modified N-E does in the temperabure and pressures ranges for which their 18-constant equation was
developed. At pressures and/or respectators above this range the
modified N-E fits experimental data batter.

Bricelite Critical Consumes

Guns, Chart, and Pramoutz (5) say " ..Effective critical constants for helium and dormal hydrogen have been determined by fitting experimental volumetric data for these gases to the generalised tables of Filzer (12). The effective critical compensators and pressure are found to depend on the temperature and on the molecular mass in a

For hydrogen they give

Sheller Squestone are indicated for neon.

Of the various methods (other than virials) for representing

the low-temperature (35° - 150° K) PVT properties of hydrogen which we investigated, the Gunn, Chueh, and Prausnitz method fits the experimental data best. When this method is used on neon in the temperature range from 70° - 120° K, it gives about as good a fit to experimental data as McCarty and Stewart's equation does. Both of these methods for predicting volumetric data fit the values of Holborn and Otto (6) (which were available when the two methods were developed) better than the data of Sullivan (14) (which were not available, and which deviate slightly from those of Holborn and Otto). In the present report, no work was done on neon below 70° K.

Although Gunn, Chueh, and Prausnitz (5) said nothing about the use of their effective critical constants at temperatures and pressures higher than the range of Pitzer's tables, we investigated the use of these constants in conjunction with the original R-K equation at higher T's and P's. In general, this procedure gave a better fit to experimental data than did the original R-K, but a poorer fit than the modified equations (See table 2).

SUMMARY

Specific modifications of the R-K equation are developed for hydrogen and for neon. The numerical coefficient in B is changed to .08063 for hydrogen and to .1025 for neon. The equation for hydrogen is recommended for temperatures from 98° to 423 ° K with pressures to 1,050 atm. The neon modification is recommended for

the low-temperature (35" - 150" K) PVT properties of hydrogen which we investigated, the Gunn, Chueh, and Frauentiz sethed fits the experimental data best. When this method is used on meon in the temperature range from 70" - 120° K, it gives about as good a fit to experimental data as McCarty and Stewart's equation does. Both of these methods for presicting volumetric data fit the values of Mciborn and Otto (6) (which were swallable when the two methods were dayeloped) better than the data of Sullivan (14) (which were not eavelable, and which dayiets alightly from those of Holborn and Otto). In the present report, no work was done on meon below and Otto). In the present report, no work was done on meon below

Although Gunn, Chuen, and Franchitz (5) said nothing about the use of their effective critical constants at temperatures and pressures higher than the range of Fitzer's tables, we investigated the use of these constants in conjunction with the original S-K equation at higher T's and P's. In general, this procedure gave a better fit to experimental data than did the original R-K, but a poorer fit than the modified equations (See table 2).

YSLAMMER

Specific modifications of the N-K equation are developed for hydragen and for mean. The numerical coefficient in B is changed to .08063 for hydrogen and to .1025 for meon. The equation for hydrogen is recommended for temperatures from 98° to 423° K with pressures to 1,050 atm. The meon modification is recommended for

temperatures from 120° to 973° K with pressures up to about 1,500 atm. Good performance is indicated above 973° K.

For temperatures lower than these, the use of the "effective critical constants" of Gunn, Chueh, and Prausnitz, in conjunction with Pitzer's tables, is suggested.

temperatures from 120° to 973° E with traceures up to about 1,300

For comparatures lower than these, the use of the "effective estimated constants" of Count, Chueh, and Proceeding in conjugation with Pitzer's tables, is suggested.

NOMENCLATURE

A = parameter of Redlich-Kwong equation

a = parameter of Redlich-Kwong equation

B = parameter of Redlich-Kwong equation

b = parameter of Redlich-Kwong equation

 $h = \frac{BP}{Z}$

K = Kelvin temperature

P = pressure, atm

P_c = critical pressure

R = universal gas constant

R-K = Redlich-Kwong

T = temperature, degrees Kelvin

 $T_{c} = critical temperature$

 $V = molal \ volume, \ cm^3/g \ mole$

Z = compressibility factor, PV/RT

NUMBERCLATURE

- A parameter of Redilok-Kwong equation
- a = parameter of Hadiuch-Kwong equation
- B parameter of Redlich-Ewong equation
- b = parameter of Redlich-Ewong equation
 - n ne
 - E = Kelvin temperature
 - P a pressure, act
 - P = oritical pressure
 - nervers and lestevine W
 - R-K = Redlich-Kuong
 - T = teseserature, degrees telvin
 - T . critical temperature
 - V = molal volume, cm /g mole
 - Z = compressibility factor, 2V/RT

ACKNOWLEDGEMENTS

The authors wish to acknowledge the valuable assistance of Miss Jo Battle, Librarian of the Helium Research Center and her staff, who ordered many of the reprints needed for this report.

We also wish to acknowledge the untiring efforts of Mr. Billy Joe King who was Digital Computer Systems Operator for the Branch of Automatic Data Processing, Helium Activity, when this work was done.

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